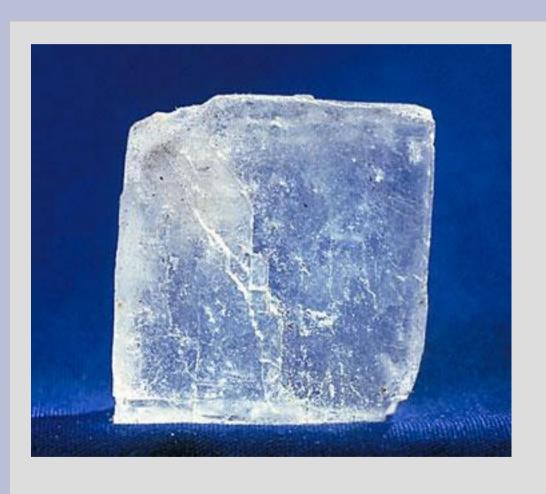
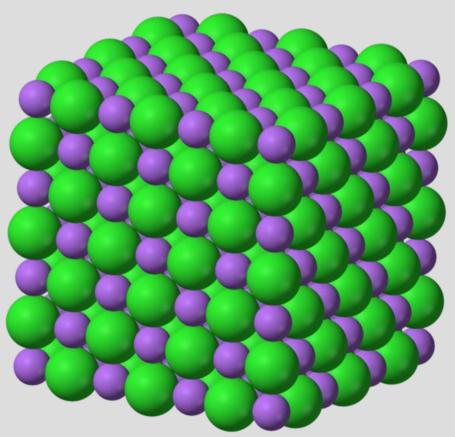


Crystals

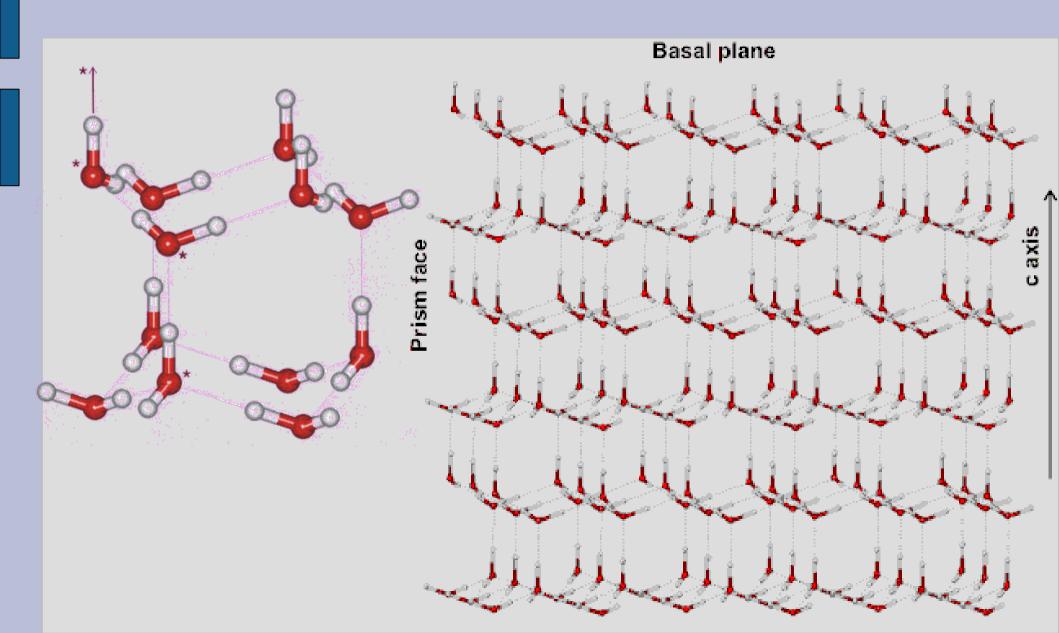


Salt (Sodium Chloride)

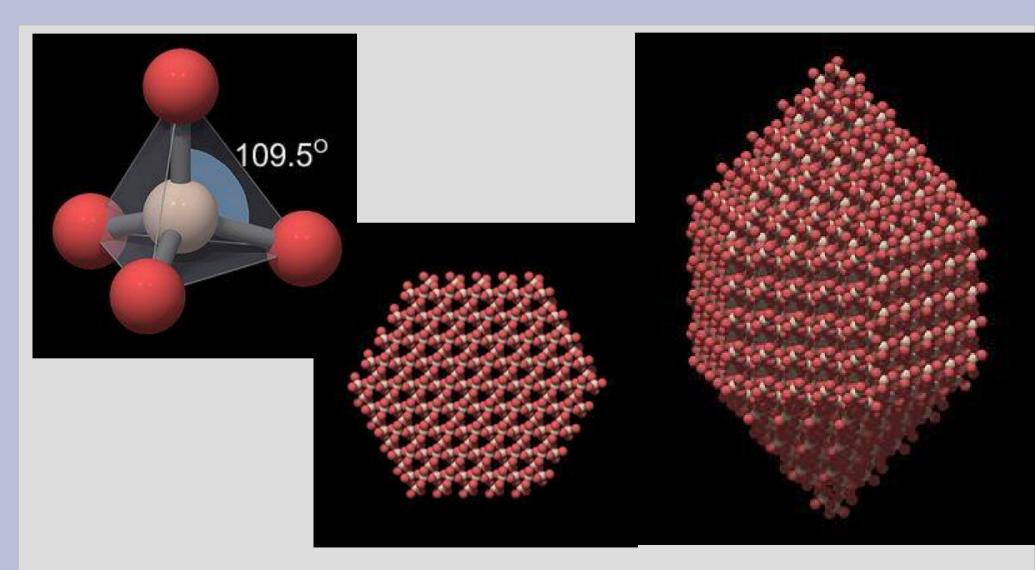




Water Ice (hexagonal Ice I_h)



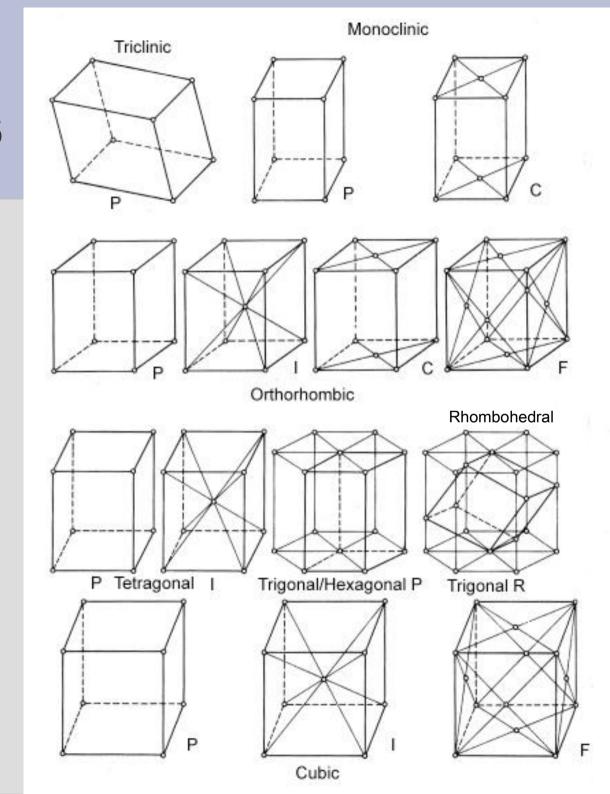
Quartz (SiO₂)

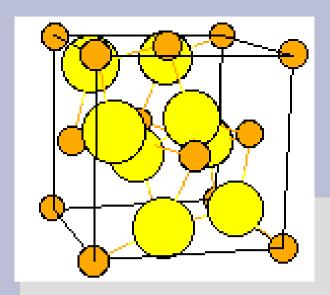


http://www.quartzpage.de/gen_struct.html

Crystal Systems

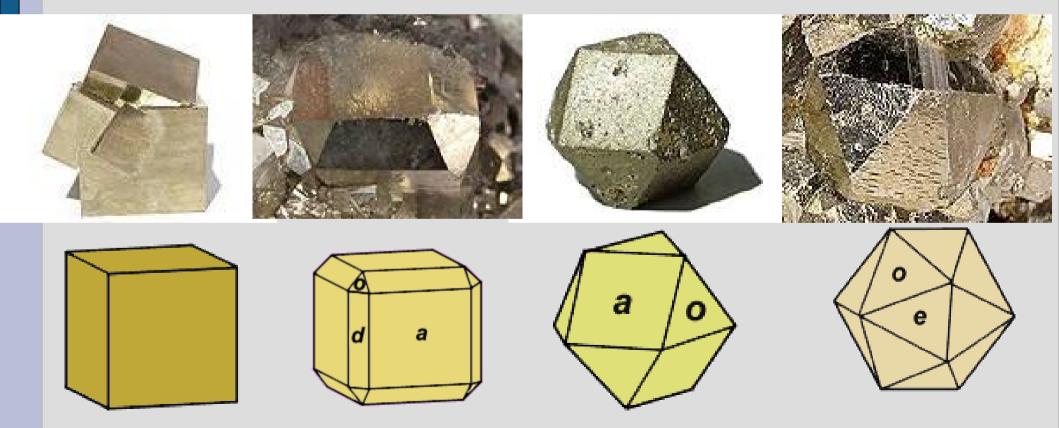
- 7 Crystal
 Systems
- 14 Bravais lattices
- 230 space groups





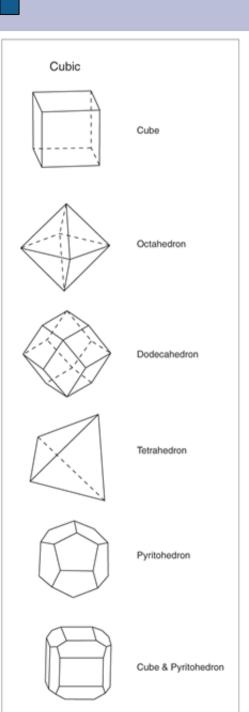
Crystal Forms of Pyrite (cubic)

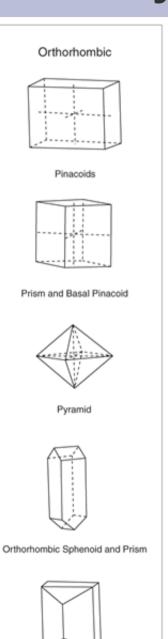
Pyrite = $FeS_2 = Fe^{2+} + S_2^{2-}$



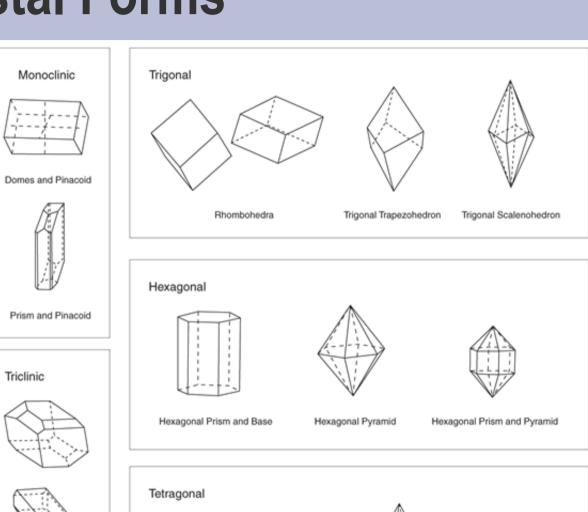
http://www.seilnacht.com/Minerale/kubisch.htm

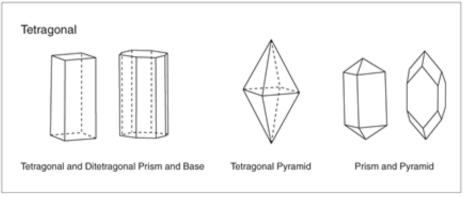
Crystal Forms





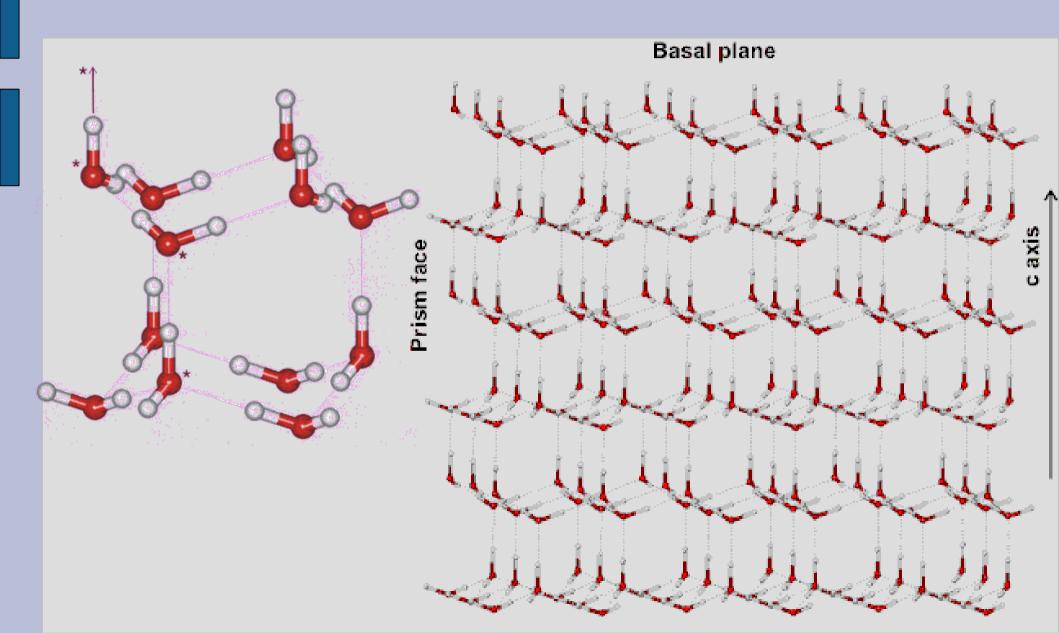
Prism, Domes and Two Pinacoids



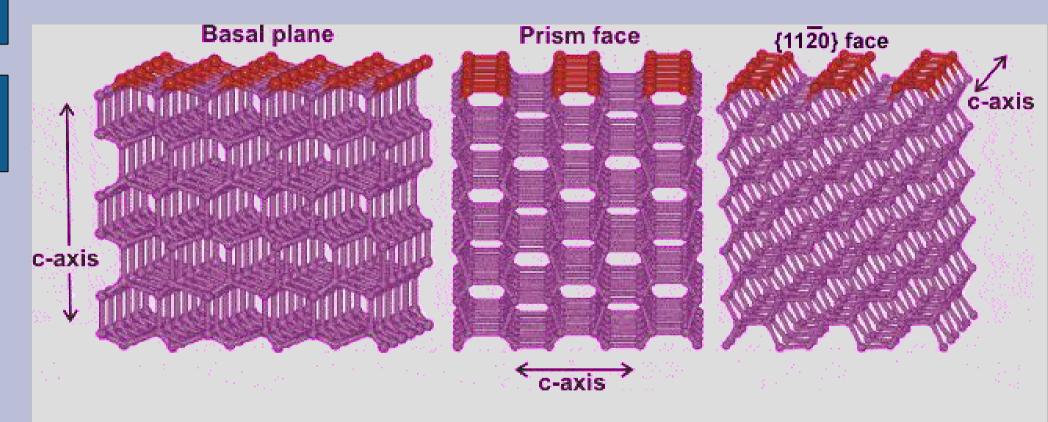


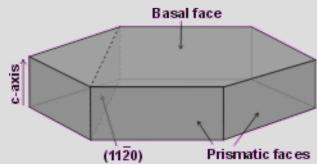
http://amonline.net.au/geoscience/minerals/crystallography.htm

Water Ice (hexagonal Ice I_h)



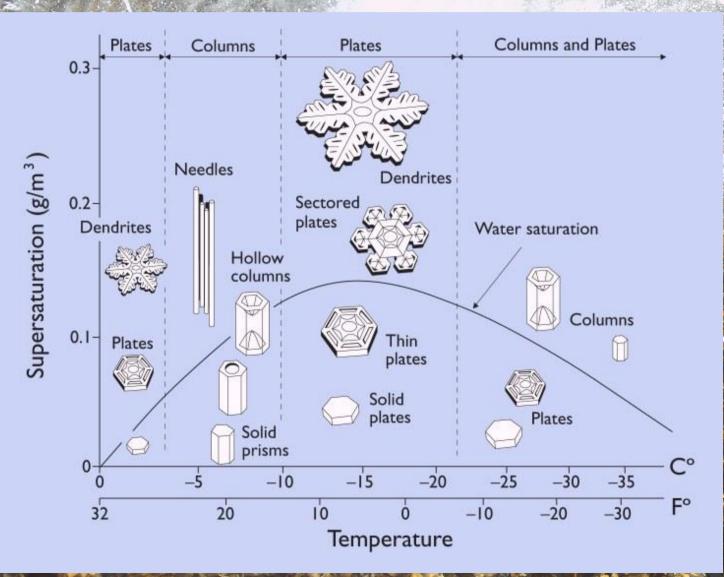
Ice Ih







Snowflake morphology (Nakaya diagram)





Snowflake morphology depends on growth conditions

- temperature
- water vapour

Diffusion-limited aggregation (DLA)

- particles undergoing random walk (diffusion, Brownian motion)
- aggregate
- no reorganization
- produce "Brownian trees"



Other fingering mechanisms

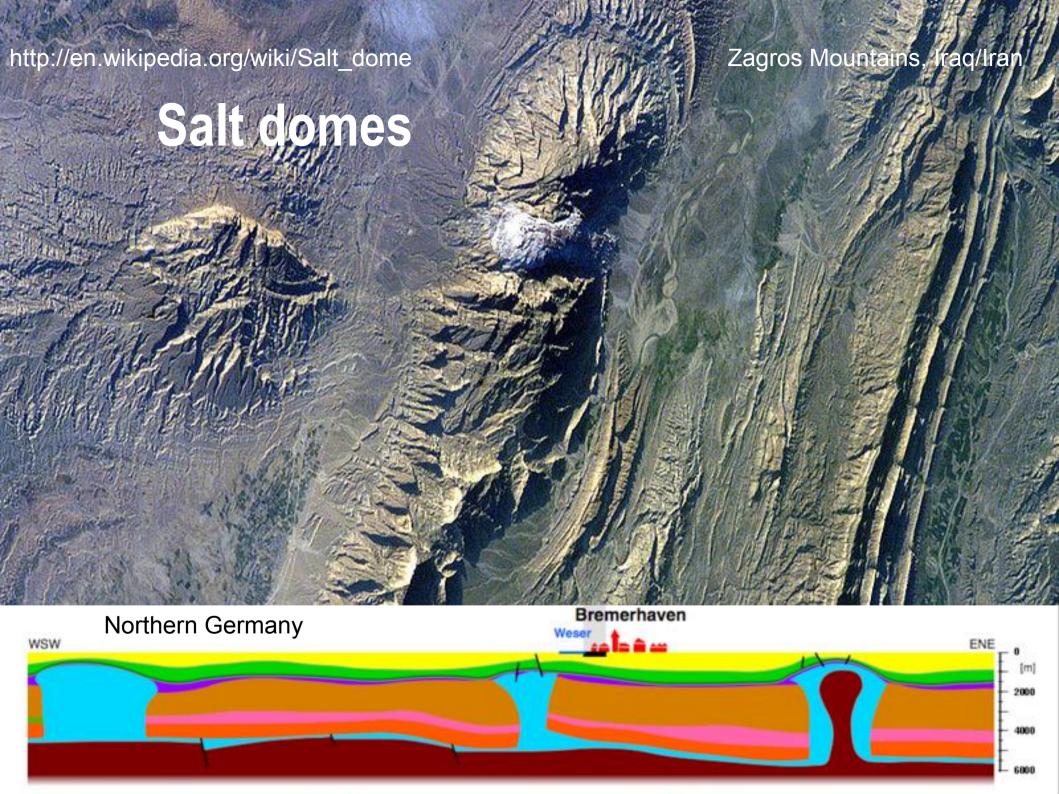
- Basic idea: Growth at the tip is easier than at the base
- A lot of different examples and names:
 - Viscuous fingering; flow in porous medium (Saffman-Taylor instability)
 - Fingering in solidification (Mullins-Sekerka instability)











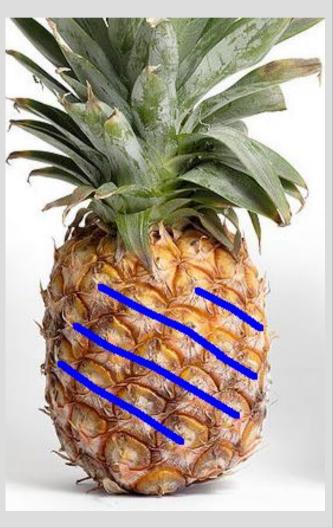


Pineapple science

How many spiral arms do you count?









Fibonacci sequence

- 1,1,3,5,8,13,21,34,55,89,144, ...
- Each number is the sum of the two predecessors



Leonardo of Pisa (c. 1170 – c. 1250), also known as Leonardo Pisano, Leonardo Bonacci, Leonardo Fibonacci

Fibonacci sequence and Golden Ratio

```
Fibonacci: 1,1,3,5,8,13,21,34,55,89,144,...
 3 / 1 = 3
 5 / 3 = 1.66666...
 8 / 5 = 1.6
 13 / 8 = 1.625
 21 / 13 = 1,61538461538...
 34 / 21 = 1,61904761905...
 55 / 34 = 1,61764705882...
 89 / 55 = 1,61818181818...
 \lim(f_n/f_{n-1}) = 1.61803398... = (1+\sqrt{5})/2
```

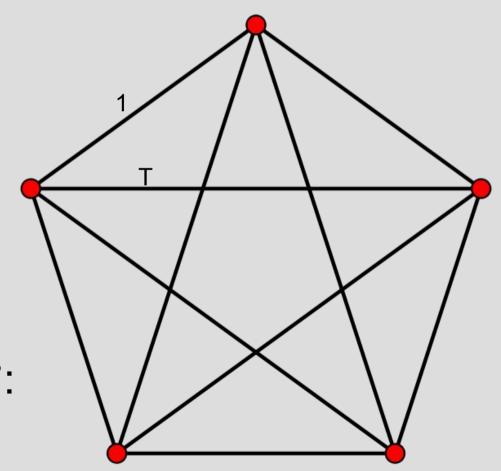
Golden Ratio

$$T = \lim(f_n/f_{n-1}) = 1.61803398... = (1+\sqrt{5})/2$$

$$T:1=(T+1):T$$

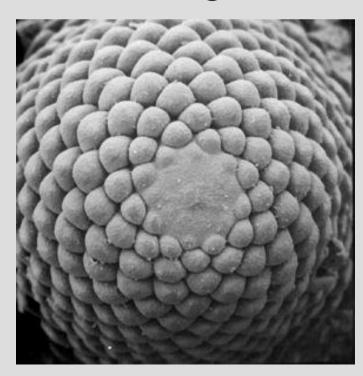
Golden angle: 360°/T ~ 222.5...°

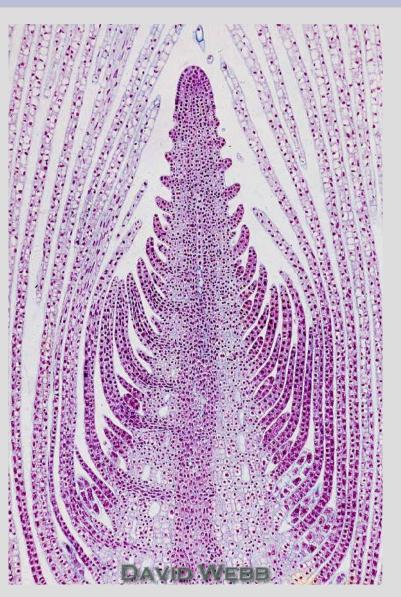
Or, more common, make it smaller than 180°: 360° - 360°/T ~ 137.5...°



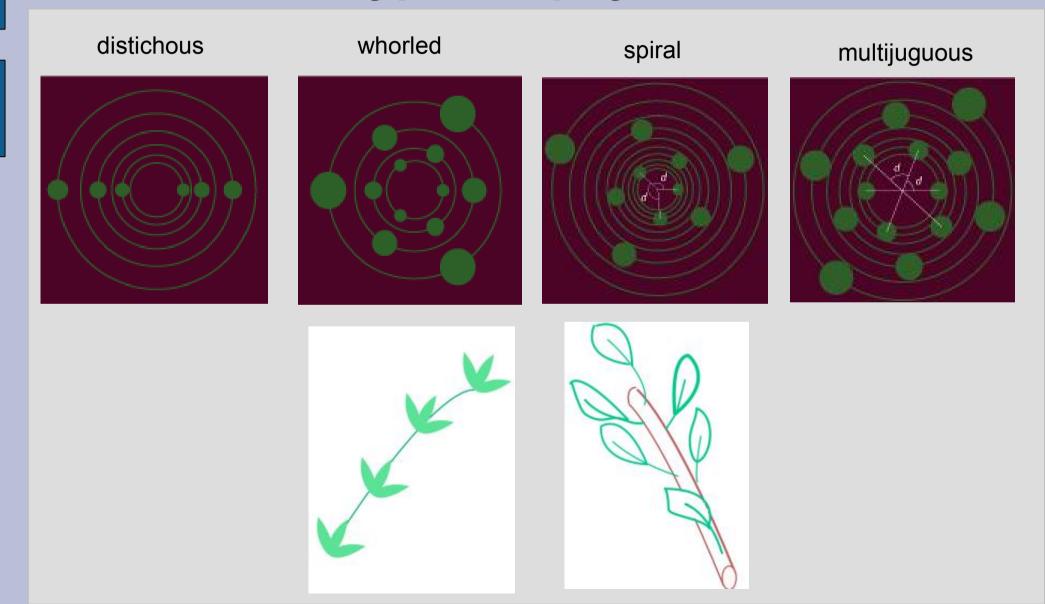
Phyllotaxis or phyllotaxy (arrangement of leaves)

- plants: modular organisms
- tip (apex) growth: new modules formed on meristematic ring





Classification: Main types of phyllotaxis

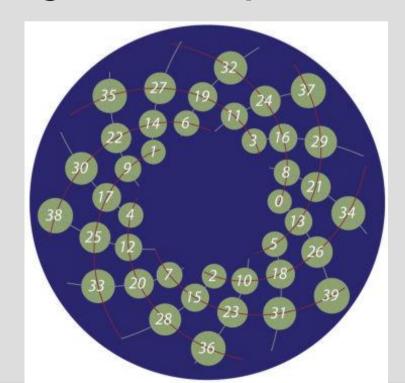


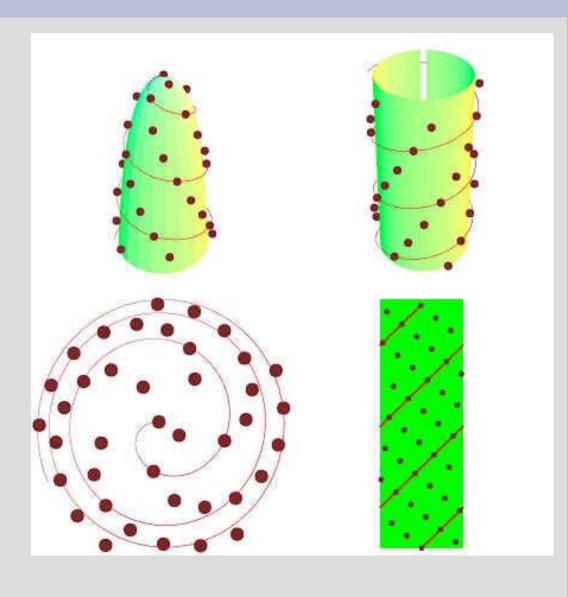




Two spirals...

- paristiche: spirals made up of next neighbours
- generative spiral



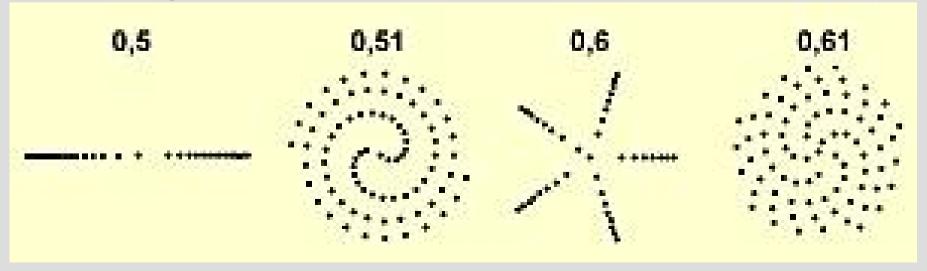


Why the golden angle?

Try different angles with the Spiral lattices applet:

http://www.math.smith.edu/phyllo//Applets/Spiral/Spiral.html

Golden angle gives the densest arrangement with least overlap



The most irrational number

There is a "most irrational" number, and it turns out (surprise, surprise) the golden number.

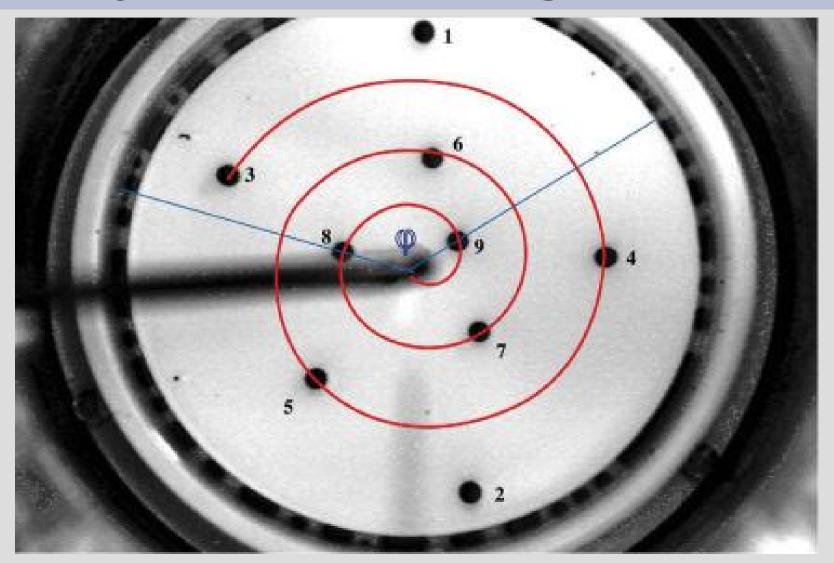
...

It is the most badly "approximable-by-rational" number there is!

Its "badness" is exceeded only by the awkwardness of the preceding sentence.

(Adam, Mathematics in Nature, p220)

An Experiment: Phyllotaxis as self-organization



Patterns in Nature Outline

- 1. Introduction
- 2. Waves and oscillations
- 3. Regularity and chaos
- 4. Animal cooperation
- 5. Spatial patterns
- 6. Aggregation and growth processes
- 7. Cellular automata
- 8. Fractals
- 9. Miscellaneous topics
- 10. Concluding session

